

Seat No.	
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Total No. of Pages : 4

**S.E. (Civil) (Part - II) (Semester - III) Examination,  
December - 2014  
ENGINEERING MATHEMATICS - III  
Sub. Code : 42654**

Day and Date : Friday, 05 - 12 - 2014

Total Marks : 100

Time : 10.00 a.m. to 01.00 p.m.

- Instructions :
- 1) Attempt any three questions from each section.
  - 2) Figures to right indicate full marks.
  - 3) Use of non programmable calculator is allowed.
  - 4) Use one answer book for both the sections.

**SECTION - I**

Q1) Solve :

a)  $(D^2 - 5D + 6)y = e^x \cos 2x$ . [6]

b)  $\frac{d^2y}{dx^2} - 2\frac{dy}{dx} + y = x \sin x$ . [5]

c)  $x^2 \frac{d^2y}{dx^2} - 2x \frac{dy}{dx} - 4y = x^4$ . [6]

Q2) The differential equation satisfied by a beam uniformly loaded (W kg/meter), with one end fixed and the second end subjected to tensile force P, is given by [16]

$$E.I. \frac{d^2y}{dx^2} = Py - \frac{1}{2}Wx^2.$$

P.T.O

Show that the elastic curve for the beam with conditions  $y = 0 = \frac{dy}{dx}$  at  $x = 0$  is given by

$$y = \frac{W}{Pn^2}(1 - \cosh nx) + \frac{Wx^2}{2P} \text{ where } n^2 = \frac{P}{EI}$$

Q3) Solve:

a)  $y^2 p - xyq = x(z - 2y)$  [6]

b)  $p^2 + q^2 = z^2(x + y)$  [6]

c)  $p(1 + q^2) = q(z - a)$  [5]

Q4) a) Given that  $f(x) = x + x^2$  for  $-\pi < x < \pi$ , find the Fourier expansion of

$f(x)$  and hence deduce that  $\frac{\pi^2}{6} = \frac{1}{1^2} + \frac{1}{2^2} + \frac{1}{3^2} + \frac{1}{4^2} + \dots$  [9]

b) Obtain half range sine series for [7]

$$f(x) = \begin{cases} x & ; 0 \leq x \leq a \\ a & ; a \leq x \leq \pi - a \\ \pi - x & ; \pi - a \leq x \leq \pi \end{cases}$$

### SECTION - II

Q5) a) Record of test of intelligence ratio (I.R.) and engineering skills (E.S.) of 10 students are given in the following table. Calculate coefficient of correlation. [5]

Student	A	B	C	D	E	F	G	H	I	J
I.R. (x)	105	104	102	101	100	99	98	96	93	92
E.S (y)	101	103	100	98	95	96	104	92	97	94

- b) In a partially destroyed laboratory record, only the lines of regression of  $y$  on  $x$  and  $x$  on  $y$  are available as  $4x - 5y + 33 = 0$  and  $20x - 9y = 107$  respectively. Calculate  $\bar{x}$ ,  $\bar{y}$  and the coefficient of correlation between  $x$  and  $y$ . [5]
- c) Fit a second degree parabola  $y = a + bx + cx^2$  to the following data: [6]

$x$	-3	-2	-1	0	1	2	3
$y$	4.63	2.11	0.67	0.09	0.63	2.15	4.58

- Q6) a) A random variable  $x$  has the following probability distributions. [6]

$x$	0	1	2	3	4	5	6	7	8
$p(x)$	$a$	$3a$	$5a$	$7a$	$9a$	$11a$	$13a$	$15a$	$17a$

Determine :

- i) The value of  $a$ ,
  - ii)  $p(x < 3)$ ,  $p(x > 3)$ ,  $p(0 < x \leq 5)$ .
- b) The probability that a bomb dropped from a plane will strike the target is  $1/5$ . If six bombs are dropped, find the probability that [5]
- i) Exactly two will strike the target,
  - ii) At least two will strike the target.
- c) Between 2 and 4 P. M. the average of phone calls per minute coming into the switch board of a company is 2.5. Use Poisson distribution to find the probability that during one particular minute there will be [6]
- i) Non phone call at all,
  - ii) Exactly 3 calls.

Q7) a) Find the directional derivative of  $f(x, y) = xy^2 + yz^2$  at the point  $(2, -1, 1)$  along the normal to the surface  $xy + yz + zx = 3$  at the point  $(1, 1, 1)$ . [5]

b) If  $\vec{r} = xi + yj + zk$  with  $r = |\vec{r}|$  and  $\vec{a}$  is a constant vector, prove that

$$\nabla \times \left( \frac{\vec{a} \times \vec{r}}{r^n} \right) = \frac{(2-n)}{r^n} \vec{a} + \frac{n(\vec{a} \cdot \vec{r})}{r^{n+2}} \vec{r}. \quad [6]$$

c) Show that the vector field defined by

$\vec{F} = (y \sin z - \sin x)i + (x \sin z + 2yz)j + (xy \cos z + y^2)k$  is irrotational and find its scalar potential. [6]

Q8) a) Verify Green's theorem for  $\int_C [(3x - 8y^2)dx + (4y - 6xy)dy]$  where  $C$  is the boundary of the region bounded by  $x = 0$ ,  $y = 0$  and  $x + y = 1$ . [8]

b) Use the Stoke's theorem to evaluate

$\int_C [(x+2y)dx + (x-z)dy + (y-z)dz]$  where  $C$  is boundary of the triangle with vertices  $(2, 0, 0)$ ,  $(0, 3, 0)$  and  $(0, 0, 6)$  oriented in the anti-clockwise direction. [8]

